

Solve the equation exactly: $\sin^2\theta - 2\sin\theta + 1, 0 \leq \theta < 2\pi$

$$x^2 - 2x + 1 = 0$$

$$(x-1)(x-1) = 0$$

$$\sin^2\theta - 2\sin\theta + 1 = 0$$

$$(\sin\theta - 1)(\sin\theta - 1) = 0$$

$$\sin\theta - 1 = 0 \quad \sin\theta - 1 = 0$$

$$\sin\theta = 1 \quad \sin\theta = 1$$

$$\frac{\pi}{2}$$

$$\frac{\pi}{2}$$

Solve the equation exactly: $2\cos^2\theta + \cos\theta - 1$, $0 \leq \theta < 2\pi$

$$2x^2 + x - 1 = 0$$

$$2\cos^2\theta + \cos\theta - 1 = 0$$

$$(2\cos\theta - 1)(\cos\theta + 1) = 0$$

$$2\cos\theta - 1 = 0 \quad \cos\theta + 1 = 0$$

$$\cos\theta = \frac{1}{2} \quad \cos\theta = -1$$

$$\frac{\pi}{3}, \frac{5\pi}{3}$$

$$\pi$$

Solve the equation exactly: $2\sin^2\theta - 5\sin\theta + 3 = 0$, $0 \leq \theta < 2\pi$

$$2\sin^2\theta - 5\sin\theta + 3 = 0$$

$$(2\sin\theta - 3)(\sin\theta - 1) = 0$$

$$2\sin\theta - 3 = 0 \quad \sin\theta - 1 = 0$$

$$\sin\theta = \frac{3}{2}$$

No sol

$$\sin\theta = 1$$

$$\frac{\pi}{2}$$

Solve the equation exactly: $\cos^2\theta + 3\cos\theta - 1$, $0 \leq \theta < 2\pi$

$$\cos^2\theta + 3\cos\theta - 1 = 0$$

$$a = 1$$

$$b = 3$$

$$c = -1$$

42, 44
45, 49

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-3 \pm \sqrt{3^2 - 4(1)(-1)}}{2(1)}$$
$$= \frac{-3 \pm \sqrt{13}}{2}$$

$$\frac{-3 + \sqrt{13}}{2} \quad \frac{-3 - \sqrt{13}}{2}$$

1.197 -3.3

Solve over the interval of $[0, 2\pi)$

$$\sqrt{2} \cos \theta - 1 = 0$$

$$\text{B) } \sqrt{3} \csc \theta - 2 = 0$$

$$4 \sin^2 \theta - 1 = 0$$

$$\text{D) } (3 \cot^2 \theta - 1)(\cot^2 \theta - 3) = 0$$

Solve over the interval of $[0, 2\pi)$

$$2\cos^2 \theta + \cos \theta = 0$$

$$\cos \theta (2\cos \theta + 1) = 0$$

$$\cos \theta = 0 \quad 2\cos \theta + 1 = 0$$

$$\theta = \frac{\pi}{2}, \frac{3\pi}{2}$$

$$2\cos \theta = -1$$

$$\cos \theta = -\frac{1}{2}$$

$$\theta = \frac{2\pi}{3}, \frac{4\pi}{3}$$

$$\csc^2 \theta - \csc \theta = 2$$

$$\text{H) } 2\sin \theta \cos \theta = \cos \theta$$

$$2\sin \theta \cos \theta - \cos \theta = 0$$

$$\cos \theta (2\sin \theta - 1) = 0$$

$$\cos \theta = 0 \quad 2\sin \theta - 1 = 0$$

$$\theta = \frac{\pi}{2}, \frac{3\pi}{2}$$

$$\sin \theta = \frac{1}{2}$$

$$\frac{\pi}{6}, \frac{5\pi}{6}$$

$$\text{J) } \frac{\sin^3 \theta}{\sin \theta} = \frac{\sin \theta}{\sin \theta}$$

$$\sqrt{\sin^2 \theta} = \sqrt{1}$$

$$\sin \theta = \pm 1$$

$$\sin \theta = 0 \quad \theta = \frac{\pi}{2}, \frac{3\pi}{2}$$

$$\sin^3 \theta = \sin \theta$$

$$\sin^3 \theta - \sin \theta = 0$$

$$\sin \theta (\sin^2 \theta - 1) = 0$$

$$\sin \theta = 0 \quad \sin^2 \theta - 1 = 0$$

$$\theta = 0, \pi$$

$$\sqrt{\sin^2 \theta} = \sqrt{1}$$

$$\sin \theta = \pm 1$$

$$\theta = \frac{\pi}{2}, \frac{3\pi}{2}$$