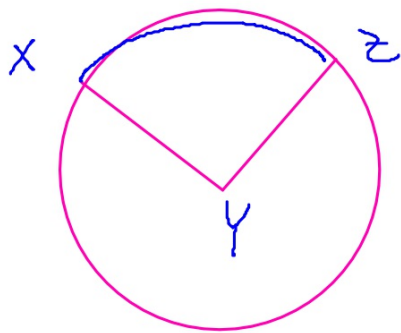


Central Angle



$$m\angle XYZ = m\widehat{XZ}$$

Intercepted Arc

## Arc Measure

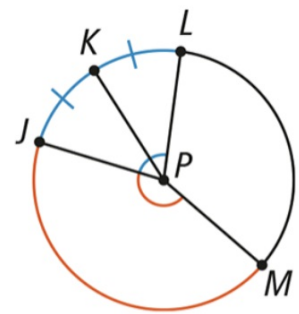
The measure of an arc is equal to the measure of its corresponding central angle.

$$m\widehat{JM} = m\angle JPM$$

Congruent central angles intercept congruent arcs, and congruent arcs are intercepted by congruent central angles.

$$\angle JPK \cong \angle KPL$$

$$\widehat{JK} \cong \widehat{KL}$$

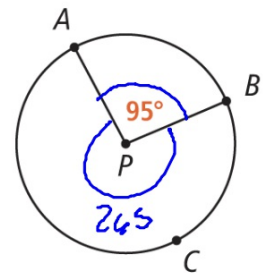


What are  $m\widehat{AB}$  and  $m\widehat{ACB}$ ?

SOLUTION

$$m\widehat{AB} = 95^\circ$$

$$m\widehat{ACB} = 265$$

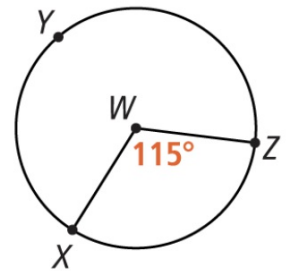


$$\begin{aligned} 360 - 95 \\ = 265 \end{aligned}$$

1. Use  $\odot W$ .

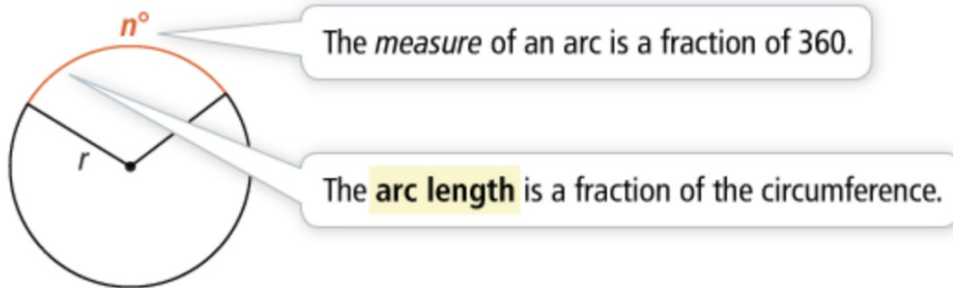
a. What is  $m\widehat{XZ}$ ?  $= 115$

Enter your answer.



b. What is  $m\widehat{XYZ}$ ?  $245$

A. How do you find the length  $s$  of an arc measured in degrees?



Use a proportion to represent the relationship between arc length  $s$ , radius  $r$ , and arc measure  $n$ .

$$\frac{\text{arc length}}{\text{circumference}} = \frac{\text{arc measure}}{360}$$
$$\frac{s}{2\pi r} = \frac{n}{360}$$
$$s = \frac{n}{360} \cdot 2\pi r$$

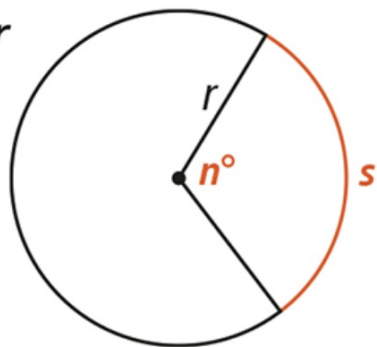
The formula to find the length of an arc is  $s = \frac{n}{360} \cdot 2\pi r$ .

## Arc Length

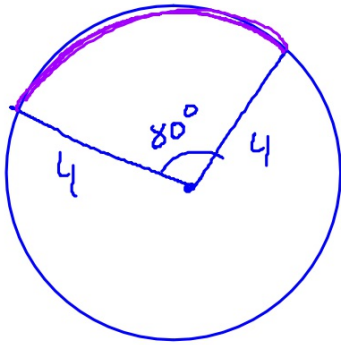
The length  $s$  of an arc of a circle is the product of the ratio relating the measure of the central angle in degrees to 360 and the circumference of the circle.

Central angle in degrees:

$$s = \frac{n}{360} \cdot 2\pi r$$



2. a. In a circle with radius 4, what is the length of an arc that has a measure of 80? Round to the nearest tenth.



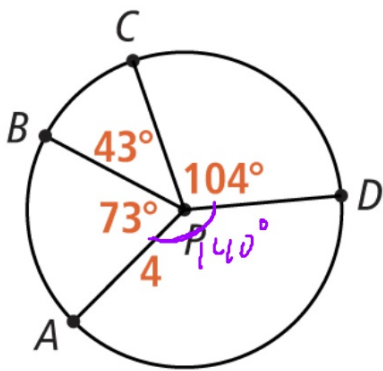
$$S = \frac{n}{360} \cdot 2\pi r$$

$$\frac{80}{360} \cdot 2\pi(4)$$

$$\frac{2}{9} (8\pi)$$

$$\frac{16\pi}{9} = 1.8\pi$$

What is the length of  $\widehat{AD}$ ? Express the answer in terms of  $\pi$ .



$$r = 4$$

$$S = \frac{n}{360} \cdot 2\pi r$$

$$= \frac{140}{360} = 2\pi(4)$$

$$= \frac{7}{18} (8\pi)$$

$$\frac{56\pi}{18} = \frac{28\pi}{9}$$